

Warmup ProblemsWarmup Problem 1

G & T Problem 4.1

 $N=5$ distinguishable spins ... $E = -\mu B$

These two

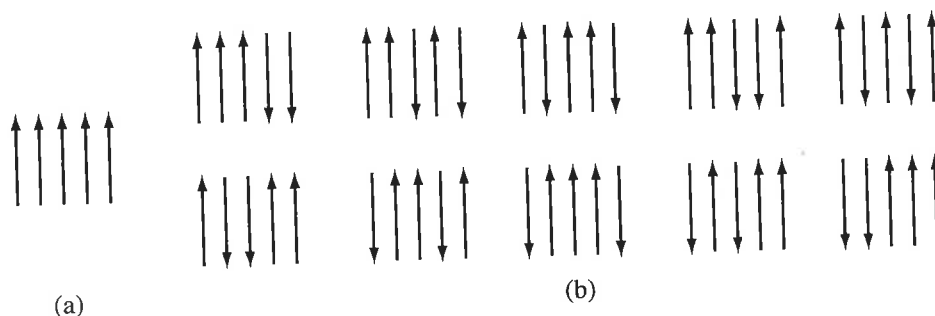
variables specify macrostate. There are ten microstates which you see in Fig. 4.1

Figure 4.1. (a) Example of an inaccessible microstate corresponding to the macrostate specified by $E = -\mu B$ and $N = 5$. (b) The ten accessible microstates. Spin 1 is the leftmost spin.

(a) What is mean value of spin "2"?

This is mean value of any single spin.

We just look at picture:

$$\bar{S}_2 = \frac{1}{2} \left(\frac{1+1+(-1)+1+(-1)+(-1)+1+1+1+(-1)}{10} \right)$$

spin of any individual S_i is $\pm \frac{1}{2}$

$$= \frac{1}{2} \left(\frac{6-4}{10} \right) = \frac{1}{2} \cdot \frac{2}{10} = \underline{\underline{+\frac{1}{10}}}$$

Note... If you solved this like example at bottom of page 181, you used $S_i = \pm 1$ so your answer would be $\underline{\underline{\frac{1}{5}}}$

These are not δ b/c The macrostate of $E = -\mu B$ biases the spins so they are more likely to be positive, making $E = -\mu B \sum_{i=1}^5 S_i = -\mu B$.

(b) Prob spin (say 2) points up is

$$P = \frac{\# \text{ states where 2 is up}}{\text{total \# states}} = \frac{6}{10} = \underline{\underline{\frac{3}{5}}}$$

(c) Given spin 1 is up, what is prob spin 2 is up?

To solve, we restrict ourselves to the 6 microstates where spin 1 is up. Of these, there are 3 where spin 2 is up.

Thus $P(\text{spin 1 up} \mid 2 \text{ is up}) = \frac{3}{6} = \underline{\underline{\frac{1}{2}}}$