

Warmup Problem

W1 Maxwell relns:

$$\alpha_p \equiv \alpha = \frac{1}{V} \left(\frac{\partial V}{\partial T} \right)_p$$

a) Maxwell relation we would use is

$$\left(\frac{\partial V}{\partial T} \right)_p = - \left(\frac{\partial S}{\partial P} \right)_T \quad \text{Thus}$$

$$\alpha = - \frac{1}{V} \left(\frac{\partial S}{\partial P} \right)_T \quad \text{The}$$

Third law states that, in the words of Simon quoted in section 18.1 of B+B :

The contribution to S by each aspect of the system in Thermodynamic equilibrium tends to zero as $T \rightarrow 0$.

Thus derivatives of S (as argued in 18.2 of B+B) must vanish. Ergo:

$$\left(\frac{\partial S}{\partial P} \right)_T \rightarrow 0 \quad \text{as } T \rightarrow 0$$

The result follows $\ddot{}$

b) We want to derive

$$\left(\frac{\partial V}{\partial T} \right)_p = - \left(\frac{\partial S}{\partial P} \right)_T$$

My favorite way is to consider relevant Thermodynamic pot'l. It will be the one that is a function of natural variables T, P . Hence: $G(T, P, N)$

Now

$$\begin{aligned}
 dG &= d(H - TS) \\
 &= d(E + PV - TS) \\
 &= dE + P dV + V dP - T dS - S dT
 \end{aligned}$$

first law

$$\underbrace{dE}_{\text{of}} = \underbrace{-P dV}_{\text{work on}} + \underbrace{T dS}_{\text{heat into}}$$

$$\begin{aligned}
 \therefore dG &= V dP - S dT \\
 &= \left(\frac{\partial G}{\partial P} \right)_T dP + \left(\frac{\partial G}{\partial T} \right)_P dT
 \end{aligned}$$

$$\text{So since } \frac{\partial G}{\partial T \partial P} = \frac{\partial G}{\partial P \partial T}$$

$$\text{we have } \left(\frac{\partial V}{\partial T} \right)_P = - \left(\frac{\partial S}{\partial P} \right)_T$$

QED